

The Quadratic Formula

Standard form of a quadratic equation

$$ax^2 + bx + c = 0$$

You cannot begin to solve a quadratic equation until it is written in standard form.

Solve for x.

$$x^2 + 3x - 17 = 0$$

When a quadratic equation cannot be factored, you can solve for x by using the quadratic formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x^2 + 3x - 17 = 0$$

$$a = 1 \quad b = 3 \quad c = -17$$

$$x = \frac{-3 \pm \sqrt{3^2 - 4(1)(-17)}}{2(1)} = \frac{-3 \pm \sqrt{9 + 68}}{2}$$

$$x = \frac{-3 \pm \sqrt{77}}{2}$$

$$x = \frac{-3 + \sqrt{77}}{2}, \quad \frac{-3 - \sqrt{77}}{2}$$

Find the roots of $3x^2 - x = 10$

$$3x^2 - x - 10 = 0$$

$$a=3 \quad b=-1 \quad c=-10$$

$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(3)(-10)}}{2(3)}$$

$$x = \frac{1 \pm \sqrt{1+120}}{6}$$

$$x = \frac{1 \pm \sqrt{121}}{6} = \frac{1 \pm 11}{6}$$

$$\begin{aligned} \frac{1+11}{6} &= 2 \\ \frac{1-11}{6} &= -\frac{5}{3} \end{aligned}$$

The roots of a quadratic equation are the special x-values that, when plugged into the given quadratic equation, make it equal to zero.